

Physics 151 Class Exercise: Kinematics Graphs - KEY

1. An expectant father paces back and forth producing the position-versus-time graph shown here.

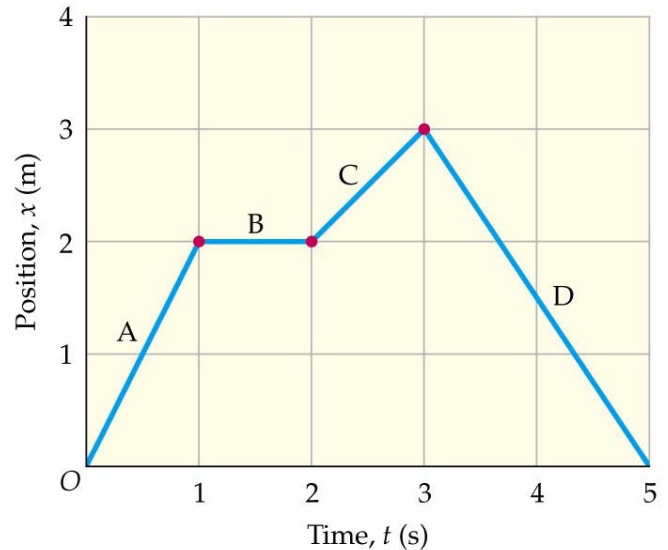
(a) Without performing a calculation indicate whether the father's velocity is positive, negative, or zero on the segments of the graph labeled A, B, C, and D.

Segment A: **Positive**

Segment B: **Zero**

Segment C: **Positive**

Segment D: **Negative**



(b) Calculate the average velocity for each segment and show that your results verify your answers to part (a).

Segment A:

Velocity is the slope of the position versus time graph

$$v_A = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i} = \frac{2\text{ m} - 0\text{ m}}{1\text{ s} - 0\text{ s}} = 2 \frac{\text{m}}{\text{s}}$$

Segment B:

$$v_B = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i} = \frac{2\text{ m} - 2\text{ m}}{2\text{ s} - 1\text{ s}} = 0 \frac{\text{m}}{\text{s}}$$

Segment C:

$$v_C = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i} = \frac{3\text{ m} - 2\text{ m}}{3\text{ s} - 2\text{ s}} = 1 \frac{\text{m}}{\text{s}}$$

Segment D:

$$v_D = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i} = \frac{0\text{ m} - 3\text{ m}}{5\text{ s} - 3\text{ s}} = -1.5 \frac{\text{m}}{\text{s}}$$

2. A motorcycle moves according to the velocity-versus-time graph shown. Find the displacement of the motorcycle for each of the segments A, B, and C.

Displacement is the area under the velocity versus time curve.

Segment A:

One could use the formula for the area of a triangle.

$$A = \frac{1}{2}bh = \frac{1}{2}(5\text{ s})\left(10\frac{\text{m}}{\text{s}}\right) = 25\text{ m}$$

or one could think about the average velocity during the time interval (0 to 5 s) which is 5 m/s. So the displacement is:

$$x = \bar{v}t = \left(5\frac{\text{m}}{\text{s}}\right)(5\text{ s}) = 25\text{ m}$$

Segment B:

Here both methods turn out to be the same. Whether one thinks about this as the area of a rectangle or the product of average velocity and time, one gets:

$$x = \bar{v}t = \left(10\frac{\text{m}}{\text{s}}\right)(10\text{ s}) = 100\text{ m}$$

Segment C:

$$x = \bar{v}t = \left(7.5\frac{\text{m}}{\text{s}}\right)(10\text{ s}) = 75\text{ m}$$

or one could add the area of the triangle plus the area of the rectangle underneath the curve.

